

# Strings and the Burrows-Wheeler Transform

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Sage/Python includes a builtin datastructure for strings. There are several ways to input strings. You can input a string using single quotes ' or double quotes ":

```
sage: s = "This is a string!"
sage: s

sage: t = 'So is this!'
sage: print(t)
```

You can also input a string using three quotes ("'' or '''). This is useful if you want to use both " and ' in your string, or you want your string to span multiple lines:

```
sage: s = """
sage: This is a multi-line
....:         string
....: that includes 'single quotes'
....:         and "double quotes".
sage: """
sage: print(s)
```

**Exercise:** Create and print the following string.

```
sage:  \ | ( | ) / /
....:  _____
....:  |               |
....:  |               |
....:  |   I <3 Coffee! /--\
....:  |               | |
....:  | \               / \--/
....:  |_____ |
```

**Exercise:** Without using cut-and-paste(!) *replace* the substring **I <3 Coffee!** with the substring **I <3 Tea!**.

**Exercise:** Print a copy of your string with all the letters capitalized (uppercase).

Strings behave very much like lists. For example,

Operation	Syntax for strings	Syntax for lists
Accessing a letter	string[3]	list[3]
Slicing	string[3:17:2]	list[3:17:2]
Concatenation	string1 \+ sting2	list1 \+ list2
A copy	string[:]	list[:]
A reversed copy	string[::-1]	list[::-1]
Length	len(string)	len(list)

**Exercise:** The *factors* of length 2 of 'rhubarb' are





Find 3 other strings that have a 'nice' image under the BWT.

**Exercise:** Is the Burrows-Wheeler transformation invertible? (That is, can you find two strings that have the same BWT?)

**Exercise:** By comparing the BWT of a string with the first column of the array of sorted rotations of a string  $s$ , devise and implement an algorithm that reconstructs the first column of the array from the BWT of  $s$ .

**Exercise:** By examining the first *two* columns of the array, devise and implement an algorithm that reconstructs the first *two* columns of the array from the BWT of a string.

(*hint:* compare the last and first column with the first two columns.)

**Exercise:** By examining the first *three* columns of the array, devise and implement an algorithm that reconstructs the first *three* columns of the array from the BWT of a string.

**Exercise:** Write a function that reconstructs the entire array of sorted rotations of a string from the BWT of the string.

**Exercise:** A *Lyndon word* is a word  $w$  that comes first in alphabetical order among all its rotations. Is the BWT invertible on Lyndon words?

**Exercise:** Explain how one can modify the BWT to make it invertible on arbitrary words. Implement your modified transformation and the inverse transformation.